

## Exercise Set 7

MA2071

(1) Find the surface area of the part of the plane  $z = 2 + 3x + 4y$  that lies above the rectangle  $[0, 5] \times [1, 4]$ .

(2) Find the surface area of the part of the surface  $z = xy$  that lies within the cylinder  $x^2 + y^2 = 1$ .

(3) Evaluate  $\int \int \int_E 2x \, dV$  where  $E = \{(x, y, z) \in \mathbb{R}^3 \mid y \in [0, 2], x \in [0, \sqrt{4 - y^2}], z \in [x, 2x]\}$ .

(4) Compute  $\int \int \int_E 6xy \, dV$  where  $E$  lies under the plane  $z = 1 + x + y$  and above the region in the  $xy$ -plane bounded by the curves  $y = \sqrt{x}$ ,  $y = 0$  and  $x = 1$ .

(5) Compute  $\int \int \int_E xz \, dV$  where  $E$  is the solid tetrahedron with vertices  $(0, 0, 0)$ ,  $(0, 1, 0)$ ,  $(1, 1, 0)$  and  $(0, 1, 1)$ .

(6) Evaluate  $\int \int \int_E x^2 \, dV$  where  $E$  is the solid that lies within the cylinder  $x^2 + y^2 = 1$ , above the plane  $z = 0$  and below the cone  $z^2 = 4x^2 + 4y^2$ .

(7) Evaluate the triple integral  $\int \int \int_B (x^2 + y^2 + z^2) \, dV$  where  $B$  is the solid unit ball  $x^2 + y^2 + z^2 \leq 1$ .